

TRANSIT MODEL OF PLANETS WITH MOON AND RING SYSTEMS

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Received 2011 May 25; accepted 2011 August 26; published 2011 November 23

ABSTRACT

Since the discovery of the first exoplanets, those most adequate for life to begin and evolve have been sought. Due to observational bias, however, most of the discovered planets so far are gas giants, precluding their habitability. However, if these hot Jupiters are located in the habitable zones of their host stars, and if rocky moons orbit them, then these moons may be habitable. In this work, we present a model for planetary transit simulation considering the presence of moons and planetary rings around a planet. The moon's orbit is considered to be circular and coplanar with the planetary orbit. The other physical and orbital parameters of the star, planet, moon, and rings can be adjusted in each simulation. It is possible to simulate as many successive transits as desired. Since the presence of spots on the surface of the star may produce a signal similar to that of the presence of a moon, our model also allows for the inclusion of starspots. The result of the simulation is a light curve with a planetary transit. White noise may also be added to the light curves to produce curves similar to those obtained by the *CoRoT* and *Kepler* space telescopes. The goal is to determine the criteria for detectability of moons and/or ring systems using photometry. The results show that it is possible to detect moons with radii as little as $1.3 R_{\oplus}$ with *CoRoT* and $0.3 R_{\oplus}$ with *Kepler*.

Key words: planets and satellites: detection – planets and satellites: rings

1. INTRODUCTION

Since the detection of the first extra-solar planet orbiting a solar-like star in 1995, 51 Peg b (Mayor & Queloz 1995), several new discoveries have been made. The most-used planetary detection methods are radial velocity and transit. Together both techniques led to the discovery of the vast majority of the over 570 planets observed so far (according to the Extra-solar Planets Encyclopaedia, <http://exoplanet.eu>). When the same planet is detected by both methods, the complete set of planetary and orbital parameters is determined. Two space missions designed to detect planetary transits are operational right now: *CoRoT*, from the CNES with a consortium of many countries, and *Kepler*, from NASA.

One of the motivations for the search of extra-solar planets is the quest for places suitable for the emergence of life. For this to be possible, the planet needs to be located in a place known as the habitable zone (Huang 1959; Kasting et al. 1993). This is the region around the host star where the radiation received by the planet is such that it allows for water to exist in its liquid state. Furthermore, the planet needs to be rocky. Due to observational bias, the majority of the planets found to date have been gaseous giants, which excludes them from being habitable even if they are in the habitable stellar zone.

Through observation of the solar system, we can infer that the existence of moons and planetary rings around gas exoplanets may be common. Also, we can deduce that moons are rocky by nature. Planetary rings may exist in very different configurations, from the rarefied rings of Uranus to the giant rings of Saturn. The detection of both moons and/or rings may uncover important clues about the planet formation and migration process. Moreover, if a gas planet located in the stellar habitable zone has moons, these moons may also be habitable, making them a good place for life to evolve.

Sartoretti & Schneider (1999) suggested that exomoons could be detected using photometry. The presence of moons

around an exoplanet would cause distortions in the transit light curve in the form of steps or asymmetries. The detection of these distortions would provide the moon's orbital parameters. Using this technique and photometric data from the *Hubble Space Telescope*, Brown et al. (2001) searched for moons and rings around the exoplanet HD 209458b. However, nothing was found. Kipping (2011) proposed an algorithm capable of analytically generating transit light curves of a planet with a moon and showed how this could be used in the search for moons using photometry. On the other hand, Han & Han (2002) studied detection possibility using gravitational micro-lensing events. Williams & Knacke (2004) showed that it is possible to detect moons orbiting gaseous giant planets in the habitable zone using spectroscopy in the 1.5–5 μm band. Kipping (2009a, 2009b) suggested that moon detection is possible from the effects on the planet motion, which may be detectable through precise measurements of the timing and duration of the transits. These are known as transit time variation and transit duration variation.

Barnes & Fortney (2004) suggested that rings around a Saturn-like exoplanet could be detected with a photometric precision of $(1-3) \times 10^{-4}$ and a time resolution of 15 minutes, as long as the ring was not viewed close to edge-on. This resolution is within the accuracy that the *Kepler* space telescope can achieve for Sun-like or brighter stars. Ohta et al. (2009) studied ring detection through photometry and spectroscopy, and concluded that rings with significantly great inclination could be detected with a radial velocity precision of 1 m s^{-1} . Schlichting & Chang (2011) studied the nature of rings that can exist around exoplanets and concluded that rings around close-in planets can show non-trivial Laplacian planes. This is caused by the increased effects of the planet's quadrupole moment. These so-called warped rings furnish important clues about the planet's interior and spin period. Despite all these proposed methods, no exomoon or planetary rings have been observed so far.

Here, we propose a model of planetary transit simulation that may be used in the search for exomoons through their signature in the light curve of their host planets. Beside the moons, the model may also simulate the transit of a planet with a ring around it. The model we propose here is capable of generating transit light curves numerically, unlike Kipping’s (2011) model. Despite the larger processing time needed to fit light curves using this method, it has the advantage of being easily adaptable to include new features, such as additional moons, changes in the ring plane, or starspots. The goal is to apply this model to the observations of the *CoRoT* and *Kepler* space telescopes, looking for the photometric signals that may indicate the presence of moons or rings around exoplanets.

Our model does not consider the detection of the warped rings shown by Schlichting & Chang (2011). Such rings are predicted around close-in exoplanets with an orbital period of a few days. Thus, our model is limited to the detection of rings located in the planet’s equatorial plane, with a larger semimajor axis. As the occurrence of such warped rings depends on the quadrupole moment J_2 and on the density of the planet, it is difficult to establish a general criterion for the validity of our model. For example, for the case of an exoplanet with density 3 g cm^{-3} and $J_2 = 10^{-2}$, warped rings occur for a semimajor axis below 0.05 AU (see Figure 6 of Schlichting & Chang 2011). Planets with a larger semimajor axis will have rings located in the planet’s equatorial plane and could be detected by our model.

The next section describes the model used in this work, whereas Section 3 presents the application of this model to a few study cases. Section 4 discusses the detectability threshold of moon and ring systems. Finally, the last section lists our main conclusions.

2. THE MODEL

The model used here is based on that of Silva (2003), where the star is considered a disk with limb darkening and the planet a completely dark disk. Both stellar and planetary parameters can be fit by the model. To minimize the number of free parameters, we consider a simple model where the moon’s orbit is coplanar with the planetary one and is also circular. Looking at the solar system’s moons, we see that these assumptions are a little limiting. However, as this is our first study on the detection of moons, we choose to consider the simplest model. In a future work, we can consider a more realistic model, including orbital inclinations and eccentricity for the moon. Regarding the planet’s eccentricity, following the strategy proposed by Kipping (2008), the model simulates elliptical orbits only for the cases where eccentricity was measured by other methods, such as radial velocities.

Stellar input parameters for the model are rotation period, radius, and mass (the latter two in solar units). The rotation period is used in the calculation of the longitude position of starspots in successive transits. We also have two limb-darkening parameters. The planetary input parameters are orbital period, radius, mass, orbital inclination angle, eccentricity, and position of the periastron. From the orbital period, the orbit’s semimajor axis is calculated by Kepler’s third law. Lastly, the moon input parameters are orbital period, radius, mass, and the angular position of the moon in its orbit at the starting time of the first transit. For the rings, the input parameters consist of inner and outer radii, and two inclination angles—one with respect to the plane of the sky and the other with the planet’s orbital plane. The transparency of the rings may also be fit.

The temporal resolution of the resulting light curve is chosen within the model by adjusting the time interval for each simulated photometric data point. Here, we used a temporal resolution of 32 s for future comparison with *CoRoT* data and 1 min for *Kepler* data.

Using stellar and planetary parameters, the planetary orbit is calculated. The line of transit is the projection of this orbit onto the stellar surface. At each time interval, the program calculates the position of the planet and its moon. The total luminosity of the star–planet–moon system is then determined by summing the intensities of all the pixels in the image where the pixels occupied by the planet and its moon have zero value. In the case of rings, the occupied pixel intensity is multiplied by the ring transparency factor. At the end of the transit, the light curve is normalized to one from the outside transit data points.

Figure 1 shows two examples of transits from the model. Figure 1(a) shows the transit of a planet and a moon in front of the star and Figure 1(b) shows the transit of a planet with rings.

It is also possible to add spots on the stellar surface, where each spot is modeled by three extra parameters: radius, intensity (with respect to stellar central intensity), and longitude position at the start of the first transit. The spot latitude is considered to be that of the projected transit line. From the stellar rotation period, the spot longitude position on consecutive transits is calculated. A further assumption is that the spot position does not change within a single transit (usually lasting a few hours), which is reasonable when the stellar rotation period is much larger than the transit duration.

2.1. Planet–Moon Dynamics

In this work, no attempt has been made at a dynamical analysis of a planet with moons or rings. Regarding planet–moon systems, we used the results of Domingos et al. (2006), where the authors used numerical simulations to obtain semiempirical expressions for the semimajor axis maximum and minimum that a satellite orbiting a giant extra-solar planet may have as a function of the stellar and planetary parameters. Domingos et al. (2006) also estimated the maximum mass of a satellite such that its orbit is stable. An interesting result is that planets with orbits very close-in to their host star can only hold moons with very small masses, but more distant planets may have stable moons with masses even larger than that of the Earth.

For example, *Rho Crb* at a distance of 0.224 AU from its host star, with an orbital period of 39.8 days, may harbor a satellite of up to $1.5 M_{\oplus}$. Farther away planets, such as HD 92788, at approximately 1 AU from its star, allow for a satellite with a maximum mass of $1 \times 10^4 M_{\oplus}$. The transiting extra-solar planets with the longest periods observed so far are *CoRoT*-9b (95.27 days), HD 80606 (114.34 days), and *Kepler*-11g (118.37 days). Thus, these planets may harbor a moon with mass similar to or even larger than Earth’s, that may be detectable from the application of the present method to *CoRoT* or *Kepler* light curves.

2.2. Planetary Transit

Figure 2 shows two examples of light curves obtained from our model. The figure on the left (a) is for the transit of a planet like HD 209458b (Southworth 2010), whereas the figure on the right (b) is for a planet similar to *CoRoT*-2b (Alonso et al. 2008).

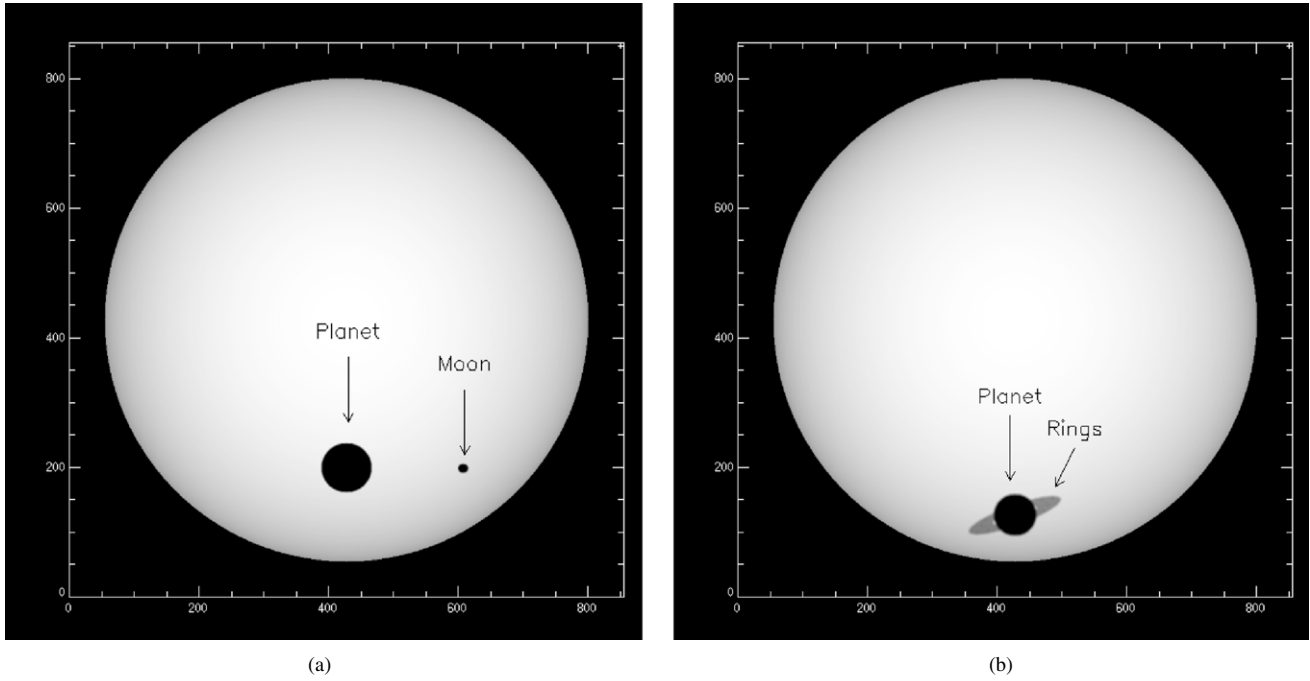


Figure 1. (a) Jupiter-like planet and a $2 R_{\oplus}$ moon transiting in front of the star. (b) Saturn-like planet with rings transiting in front of the star. The rings have the same dimensions as Saturn’s. The angle with the sky plane is 78° and the angle with the orbital plane is 20° . Both images were obtained from the model.

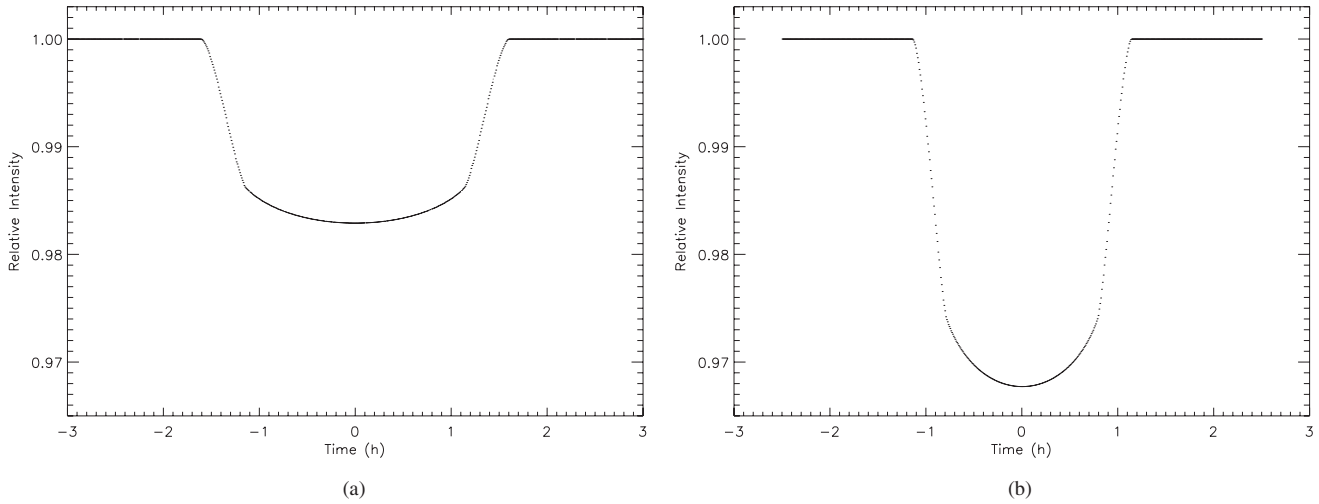


Figure 2. Transit model of two planets. (a) HD 209458b ($R = 1.38 R_J$, $P = 3.524$ days, and $i = 86^{\circ}.59$) and (b) CoRoT-2b ($R = 1.465 R_J$, $P = 1.743$ days, and $i = 87^{\circ}.84$).

2.3. Transit of a Planet with a Moon

Figure 3 shows two examples of light curves of a planet with an orbiting moon. Both panels are for a Jupiter-sized planet transiting a star identical to the Sun with an orbital period of 45 days. In the model, the added moon around this planet has two Earth radii. In Figure 3(a), the moon’s orbital period is 5 days, while in Figure 3(b) it is 2 days. Also, the position angle of the moon with respect to the planet is 0° in the first case and 60° in the second one.

When adding a moon around a planet in the model, two characteristic signatures may occur. The first one is a step, which may appear at the beginning or at the end of a transit, while the second effect is a discontinuity, a jump, seen in the bottom of the transit. The step at the beginning (see Figure 3(a)) occurs when the moon’s ingress happens before that of the planet, while the step near the end of the transit (Figure 3(b)) is caused by the

moon’s egress after the planet. Both effects are marked with an upward arrow.

Furthermore, when the moon’s orbital period is small, an asymmetry arises in the bottom of the transit, shown by the downward arrows in Figure 3. This asymmetry is generated when the moon is eclipsed by the planet. It may also happen if, at the start of the transit, the moon is already behind (or in front of) the planet, but falls out of eclipse during the transit. The width and intensity of this signal depends on the moon’s relative orbital period, radius, and also on the position angle φ of the moon with respect to the planet at the initial transit time.

2.4. Transit of a Planet with Rings

Figure 4 presents the modeled light curve produced by a transiting Saturn-like planet around a star with solar parameters

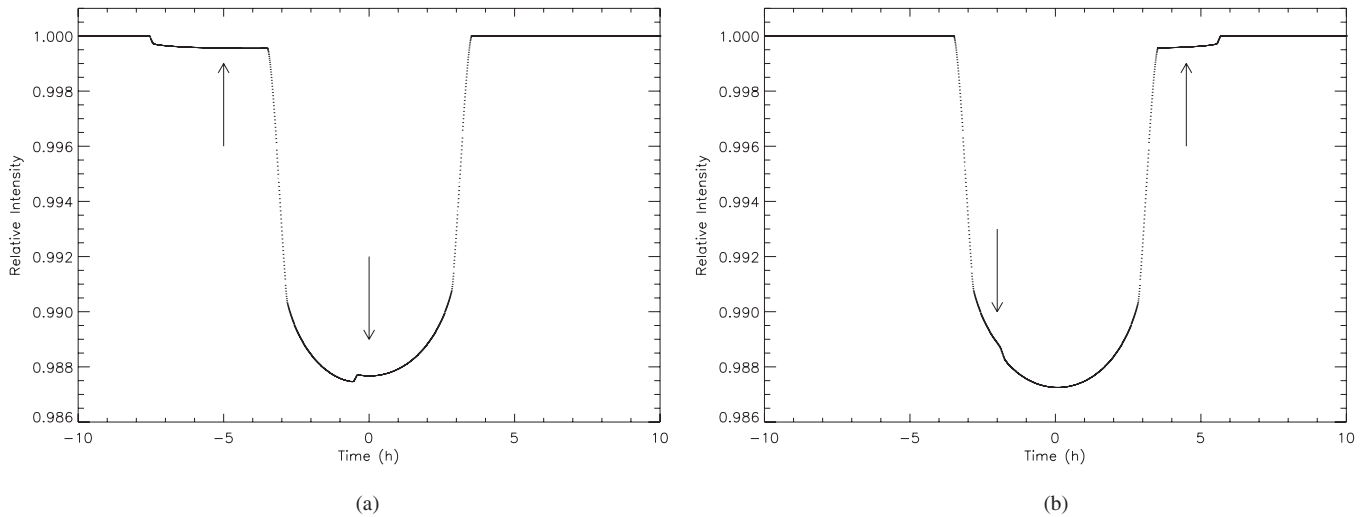


Figure 3. Model light curve of a transiting hot Jupiter ($R = 1 R_J$, $P = 45$ days, and $i = 89.5^\circ$) around a Sun-like star and an orbiting moon with $2 R_\oplus$. The moon period and position angle are, respectively, (a) $P_M = 5$ days and $\varphi = 0^\circ$; (b) $P_M = 2$ days and $\varphi = 60^\circ$.

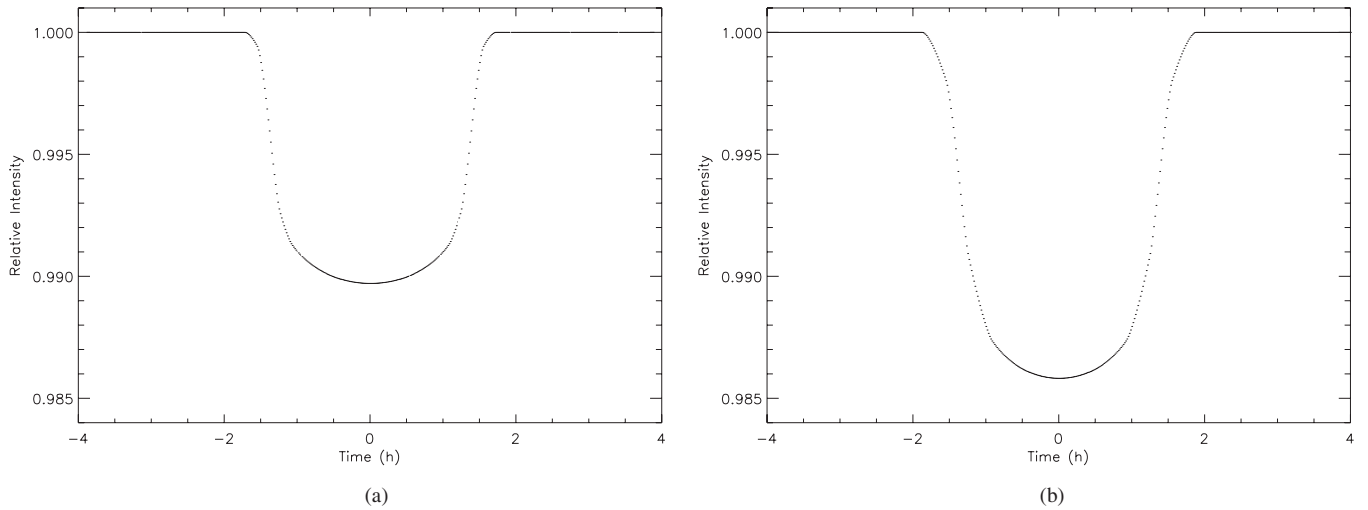


Figure 4. Transiting Saturn-like planet ($R = 0.84 R_J$, $P = 5$ days, and $i = 88^\circ$) in front of a solar-like star. Planetary rings with sizes (a) equal to and (b) increased by 50% with respect to those of Saturn.

(left panel). To enhance the signal produced by the presence of rings, their size was augmented by 50% (right panel).

The main effect of the planetary ring system is to increase the covered area of the stellar surface, the result of which is to deepen the transit light curve. Moreover, the transit shape becomes rounder at the ingress and egress instants, than it does if no rings are present. Both these factors depend strongly on the ring transparency, being larger in the case of more opaque rings, as expected.

An interesting effect appears when the ring size is increased. In this case, the light curve becomes more triangular, similar to the light curves produced during grazing eclipses of binary star systems.

2.5. Starspots

If the star has one or more spots on its surface, similar to sunspots, Silva (2003) has shown that the photometric light curve during a planetary transit will display a small “bump.” This occurs because when the planet occults a darker region of the stellar surface, occupied by the spot, there is a relative increase in the total intensity. Moreover, the detection of the

same starspots on different transits may be used to determine the rotation period of the star (Silva-Valio 2008).

Figure 5 shows the same light curves from Figure 2, except now a spot was added to the stellar surface. This spot, located at 30° longitude (measured from the center of the star), has a size of half of each planet radius and a relative intensity of 0.6 times the stellar central intensity.

In some cases, the photometric signal produced by the presence of moons may be mistaken by that caused by starspots. Distinguishing between the two cases is possible when successive transits are observed since the spots signal will have a periodicity equal to the stellar rotation period, while those of the moons will have a different period, following its own orbital period.

Examples of how confusing things can get, especially how the presence of starspots may hinder the detection of moons, are shown in Figure 6. The figure presents the transit of a planet with an orbiting moon in front of a star, in whose surface there is a spot, for two situations: only one spot (Figure 6(a)) and four spots (Figure 6(b)). In both panels, the planet is identical to Jupiter with a period of 45 days and the moon has a $3 R_\oplus$ and an orbital period of 2 days around the planet. In the case of

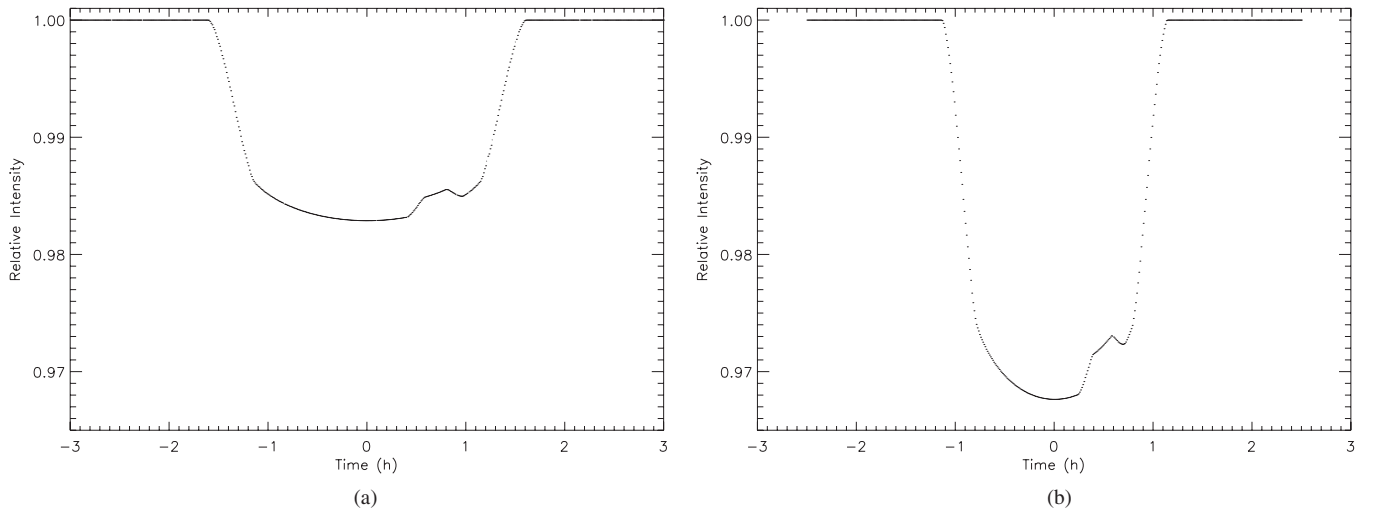


Figure 5. Planetary transit light curves for (a) HD 209458b and (b) CoRoT-2b, where the “bump” in the bottom of the transit indicates the presence of a spot on the stellar surface. In each case, the spot has half the planet radius and intensity 0.6 and is located at 30° with respect to the star center.

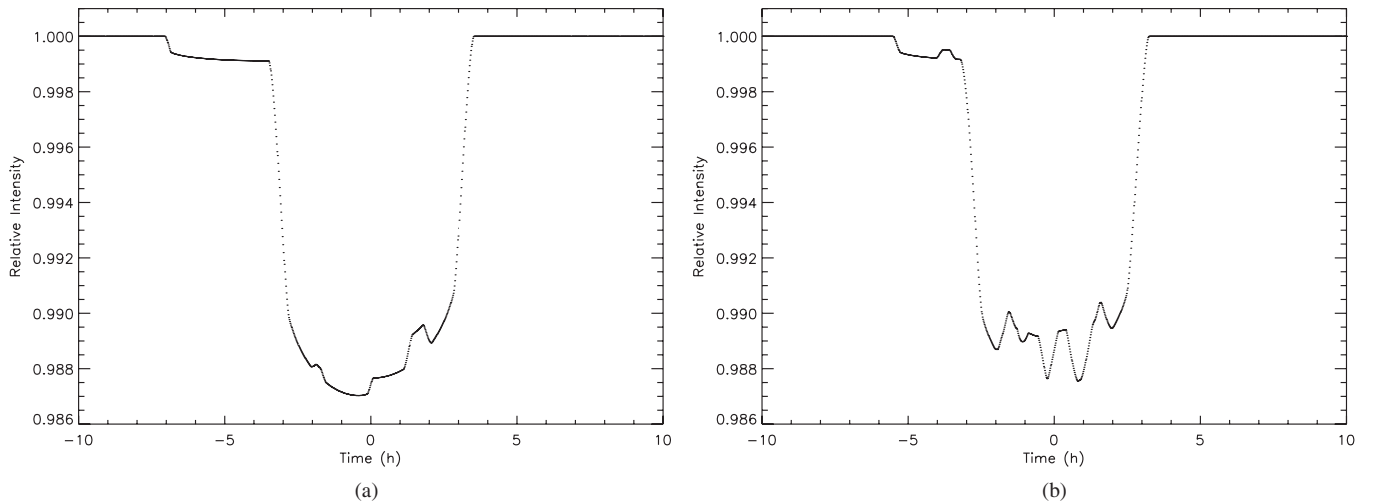


Figure 6. Jupiter-like transiting planet ($R = 1 R_J$, $P = 45$ days, and $i = 89.5^\circ$) with a $3 R_\oplus$ moon around a star equal to the Sun. (a) The star has a spot with 0.5 planet radius, intensity 0.6, located at 30° . (b) The star has four spots, with radii, respectively, 0.7, 0.6, 0.7, and 0.8 planet radius; intensity 0.6, 0.5, 0.6, and 0.7; located at -30° , -15° , 5° , and 30° . Each spot signal appears duplicated, once when the moon occults it and again when the planet eclipses the spot.

Figure 6(b), it is clearly seen that the presence of starspots can significantly complicate the detection of any moon effect on the light curve.

3. TEST RESULTS FROM THE MODEL

To verify the detectability of moon and ring systems around a planet, it is possible to add Gaussian noise to the modeled light curve and then try to recover the input parameters from a fit. For *CoRoT* data simulation, we used a noise level of 6×10^{-4} , such as that observed for *CoRoT-2* (Silva-Valio & Lanza 2010), and in the case of the *Kepler* data, 2×10^{-5} .

Once the noise has been added to the model light curve, we fit this light curve with the following sequence of algorithms. First the PIKAIA (Charbonneau 1995) algorithm is used to obtain a first guess that is then input into the AMOEBA (Nelder & Mead 1965) routine. PIKAIA is an algorithm, the main advantage of which is to find the global maximum of the function to be maximized, using only the allowed interval value for each free parameter. These results are then used as input to the AMOEBA routine that refines the result using the simplex method for convergence minimization. The error estimates for

the fitted parameters were obtained using the MPFIT algorithm (Markwardt 2009).

After the fitting procedure, we compute the goodness-of-fit using the parameter Q , as defined in Press et al. (1992) as the probability that the chi-square should exceed a particular value χ^2 by chance and calculated by

$$Q(\chi^2|\nu) = 1 - P\left(\frac{\nu}{2}, \frac{\chi^2}{2}\right), \quad (1)$$

where P is the incomplete gamma function $P(a,x)$. Generally, if Q is larger than 0.01, then the fit is acceptable. In this case, it can be said that such an event (moon or ring) is detectable. If Q is between 0.001 and 0.01, then the fit may or not be acceptable, and more studies of the noise are required. This can be caused, for example, if the measurement errors are underestimated. Q below 0.001 indicates a bad fit. On the other hand, Q very close to 1 is also not expected. This is, literally, too good to be true. This can be caused by a non-normal error distribution or overestimated measurement errors. Next, we show some examples of the fit to light curves with noise added and the results they yield.

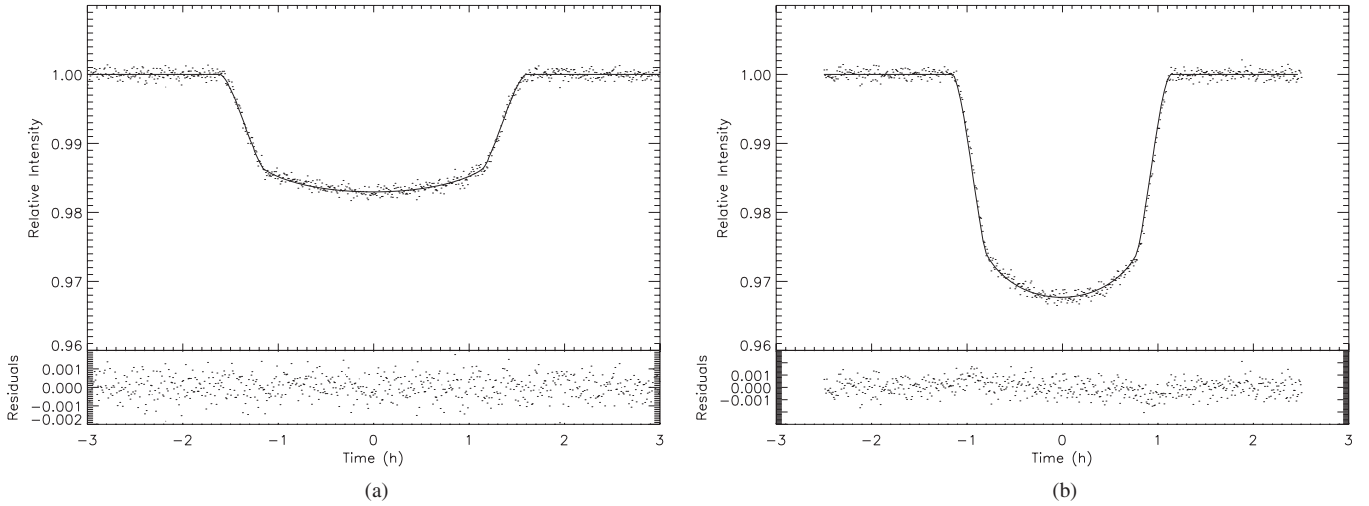


Figure 7. Light curve fit of model planetary transit for (a) HD 209458b and (b) CoRoT-2b. The dots represent the noisy light curve data points, whereas the solid line shows the best-yield fit.

Table 1
Fit Results for Planetary Transits of HD 209458b and CoRoT-2b for *CoRoT* Simulations

Planet	Parameter	Original Value	Fit Result	Reduced χ^2	Q
HD 209458b	Planet radius (R_J)	1.38	1.382 ± 0.025	1.0639	0.098
	Orbital inclination ($^\circ$)	86.59	86.6 ± 0.3		
CoRoT-2b	Planet radius (R_J)	1.465	1.466 ± 0.016	1.0157	0.3890
	Orbital inclination ($^\circ$)	87.84	87.84 ± 0.21		

Table 2
Fit Results for Planetary Transits of HD 209458b and CoRoT-2b for *Kepler* Simulations

Planet	Parameter	Original Value	Fit Result	Reduced χ^2	Q
HD 209458b	Planet radius (R_J)	1.38	1.3797 ± 0.0011	1.0627	0.1747
	Orbital inclination ($^\circ$)	86.59	86.594 ± 0.015		
CoRoT-2b	Planet radius (R_J)	1.465	1.4636 ± 0.0007	1.1156	0.0859
	Orbital inclination ($^\circ$)	87.84	87.839 ± 0.009		

3.1. Fit of a Planetary Transit

The first test to the model is to apply it to the two transiting planets described in Section 2.2, where Gaussian noise has been added similar to that of *CoRoT* and *Kepler* observations. In this fit, all the stellar parameters and the orbital period (or semimajor axis) of the planet were fixed, and the only free parameters were the planetary radius and the orbital inclination angle.

The comparison between the original parameters and those obtained from the fit of the noisy modeled light curve are seen in Tables 1 and 2, and in Figures 7(a) and 7(b) for HD 209458 and CoRoT-2. Both light curves had a noise level similar to that of the *CoRoT* satellite. The two panels show the simulated data points as dots and the fit as a solid line. The residuals are shown in the lower part of each panel.

3.2. Transit Fit of a Planet with Moon

If the planet has a moon in orbit around it, there are two factors that make its detection difficult. The first one is the noise, as expected. In cases where the moon is very small, its signature in the light curve is flooded by the noise level, leaving it undetectable. Another difficulty is the presence of starspots on the stellar surface, mentioned above.

To demonstrate how moons can be detected, we consider the case of a hot Jupiter with a period of 45 days around its

host star, modeled with no spots. In orbit around this planet there is a moon with $3 R_\oplus$ and a period of 5 days. Simulations were performed for noise levels of both *CoRoT* and *Kepler*. The parameters obtained from the fit and the original ones are listed in Table 3, whereas the fit results are plotted in Figure 8, for *CoRoT* noise level. The fit was performed for five consecutive transits, but the figure shows only the first.

We noticed that the larger the number of transits considered in the fit, the smaller the number of iterations necessary for the fitting algorithms to obtain a good fit, that is, the easier it is to detect the moon.

3.3. Transit Fit of a Planet with Rings

As seen above, planetary rings can be detected by the round shape of the transit at ingress and egress times, besides the larger depth of the transit (due to the increase in the stellar surface area covered). For these signatures to be detectable, the noise is the predominant factor. If the signature is too small, the noise will completely overcome it.

To exemplify, we simulate the transit of a planet identical to Saturn and its rings, with a 30 day period and 89° orbital inclination. The transit is modeled for two cases: one with the noise level of *CoRoT* and the other with that of the *Kepler* telescope. In both cases, the light curve was submitted to a fit

Table 3
Fit Result of Five Transits of a Planet with an Orbiting Moon

Noise Level	Parameter	Original Value	Fit Result	Reduced χ^2	Q
<i>CoRoT</i>	Planet radius (R_J)	1.0	0.9976 ± 0.0005	1.0070	0.3954
	Moon period (days)	5.0	5.001 ± 0.012		
	Moon radius (R_\oplus)	3.0	2.979 ± 0.019		
	Moon position angle ($^\circ$)	0.0	0.21 ± 0.11		
<i>Kepler</i>	Planet radius (R_J)	1.0	0.9999 ± 0.0007	1.0419	0.1337
	Moon period (days)	5.0	5.000 ± 0.023		
	Moon radius (R_\oplus)	3.0	2.999 ± 0.024		
	Moon position angle ($^\circ$)	0.0	-0.4 ± 0.6		

Table 4
Fit Results for a Saturn-like Planet Simulation, Considering Only the Planet

Noise level	Parameter	Original Value	Fit result	Reduced χ^2	Q
<i>CoRoT</i>	Planet radius (R_J)	0.84	0.934 ± 0.022	1.0291	0.2050
	Orbital inclination ($^\circ$)	89	89.0 ± 0.4		
<i>Kepler</i>	Planet radius (R_J)	0.84	0.9434 ± 0.0009	25.10	0
	Orbital inclination ($^\circ$)	89	88.999 ± 0.019		

Table 5
Resulting Parameters for the Case of a Transiting Saturn, as Would be Observed by *Kepler*

Parameter	Original Value	Fit Result	Reduced χ^2	Q
Planet radius (R_J)	0.84	0.839 ± 0.005	1.0173	0.3553
Orbital inclination ($^\circ$)	89	89.00 ± 0.03		
Inner radius (R_P)	1.11	1.11 ± 0.06		
Outer radius (R_P)	2.32	2.316 ± 0.026		
Angle with the sky plane ($^\circ$)	78.0	77.9 ± 1.5		
Angle with the orbital plane ($^\circ$)	20.0	19.9 ± 0.5		
Transparency	0.5	0.51 ± 0.06		

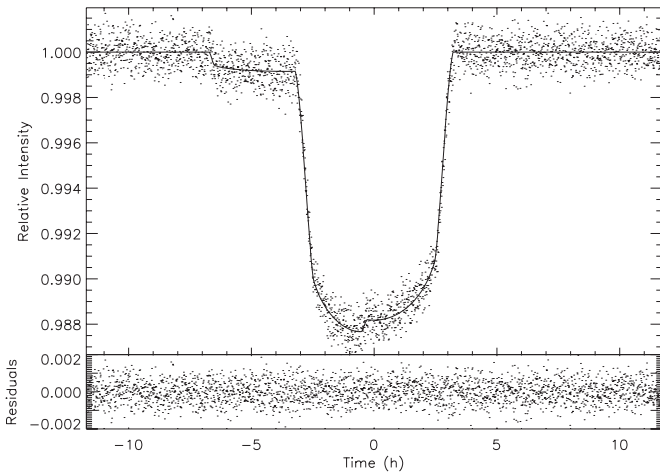


Figure 8. Light curve fit for the first transit of a hot Jupiter ($R = 1 R_J$, $P = 45$ days, and $i = 89^\circ.5$) with a moon ($R_M = 3 R_\oplus$ and $P_M = 5$ days) considering the noise level of *CoRoT*.

process assuming only the presence of the planet. The result of this preliminary fit is shown in Figure 9 and Table 4.

From the analysis of the residual plotted on Figure 9 and the Q value in Table 4, we see that the fit considering only the planet yields a satisfactory result only for the *CoRoT* noise level (Figure 9(b)). This indicates that a ring system such as that of Saturn could only be detected by the *Kepler* satellite. The *CoRoT* satellite would identify this light curve as that produced

by a giant planet with a radius slightly larger than that of Saturn (12.3 %), but without rings.

Next, we fit only the light curve plotted in Figure 9(b) but now considering the presence of rings, that is the ring parameters are taken into account. The resulting fit parameters are listed in Table 5, whereas the result of the fit is plotted in Figure 10. Comparing the residual of Figures 9(b) and 10, one can see that the fit is much better for the model where the rings were included.

The Q value in Table 5 and the residuals in Figure 10 show that the fit was satisfactory.

4. DETECTION LIMITS

To determine the radius of the smallest detectable moon, several simulations were performed decreasing the radius at each run. Every simulation had its light curve fitted yielding the moon parameters. Whenever the Q value indicates a good fit, we consider the moon detectable. Thus, in the case of *CoRoT*, the smallest detectable moon in orbit around a Jupiter-sized planet has a radius of $1.3 R_\oplus$, while in the case of *Kepler*, this minimum radius decreases to $0.3 R_\oplus$. The latter moon would be smaller than Ganymede, the larger moon of our solar system, the size of which is $0.41 R_\oplus$. In all the simulations, the star was considered Sun-like with no spots.

For the case of planetary rings, the process is slightly different, because, in this case, the biggest problem is distinguishing between single planets and those with rings. In this case, then, we adopt a criterion that takes into consideration the residuals. When fitting the light curve of a planet with rings, first only the

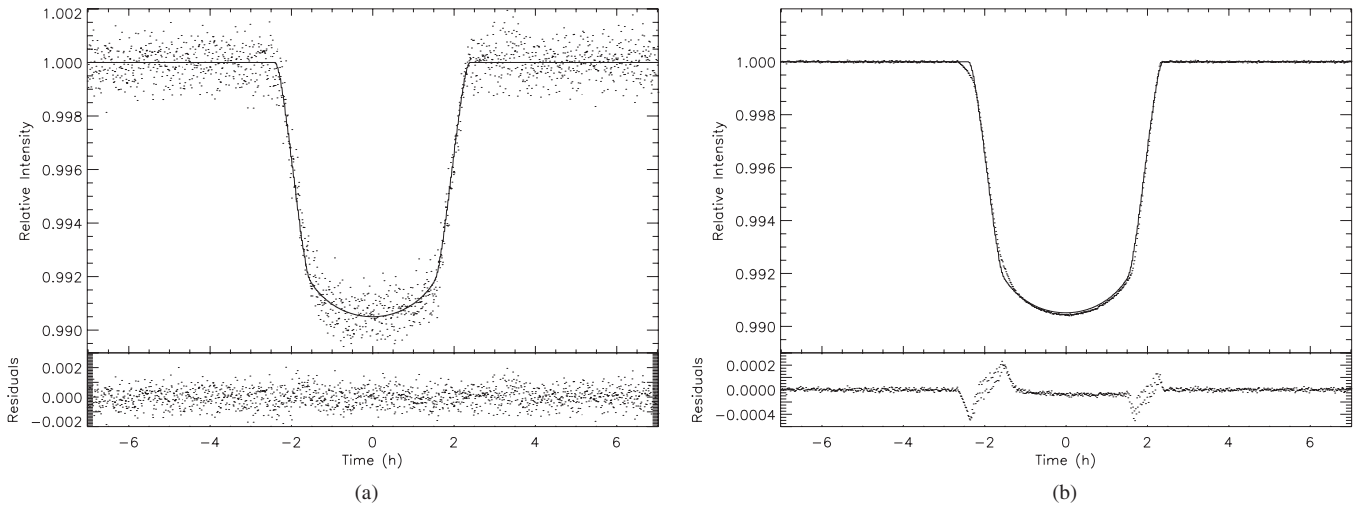


Figure 9. Saturn-like planet ($R = 0.84 R_J$, $P = 5$ days, and $i = 88^\circ$) transit fitted without considering the presence of its rings for noise levels of the (a) *CoRoT* and (b) *Kepler* telescopes, respectively.

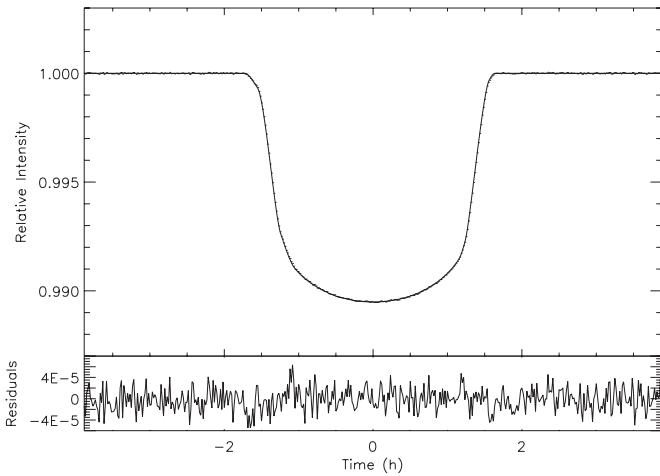


Figure 10. Saturn-like planet ($R = 0.84 R_J$, $P = 5$ days, and $i = 88^\circ$) transit fitted, considering now the presence of rings.

planet parameters are fit. If the Q value indicates a bad fit, then we may conclude that the rings can be detectable.

To establish a detectability criterion, first we define the effective area of the rings as the ring projection on the plane of the sky multiplied by its opacity, according to

$$A_{\text{eff}} = (R_E^2 - R_I^2) \pi \cos \psi (1 - \tau), \quad (2)$$

where R_I and R_E are the internal and external radii, respectively, ψ is the inclination angle of the rings relative to the plane of the sky, and τ is the transparency. Totally transparent rings have $\tau = 1$, whereas totally opaque ones have a zero value of transparency.

The results of our simulations showed that in the case of the *Kepler* data, planetary rings are detectable when the effective area corresponds to approximately 3% of the area covered by the planet. For example, rings with $\tau = 0.5$ and an inclination angle of 78° with the plane of the sky in orbit around a Saturn-like planet, will be detectable with rings about 51% the size of those of Saturn. For the *CoRoT* data, the effective area corresponds to approximately the area of the planet. Therefore, for the same planet as in the previous case, the rings should have sizes 45% larger than those of Saturn to be detectable above the *CoRoT* noise level.

5. CONCLUSION

Here we reported the results of a model capable of simulating planetary transits, including the effect of existing moons and rings around that planet. Light curves were presented for each case. Estimates of the threshold detection for such events were made. It was shown how these events may be detected using the PIKAIA and AMOEBA routines for curve fitting. As expected, the main limiting factor for the possible detection is the noise level of the telescopes. This can be seen by comparing the results from simulations of photometric light curves of *CoRoT* and *Kepler*.

The *CoRoT* data allow for the detection of moons with at least $1.3 R_\oplus$ in size around a planet identical to Jupiter. In the case of *Kepler* data, this detection limit on the moon radius drops to $0.3 R_\oplus$. For planetary rings, a Saturn-like planet would be detectable with *Kepler*; however, this same planet–ring system would be mistakenly inferred as a single planet with a slightly larger radius by *CoRoT*. Detection limits for both telescopes were estimated above.

Next, this model will be applied to real light curves to search for the types of signatures described in this work. Data from both *CoRoT* and *Kepler* will be used. An improvement that can be made to the model is the implementation of analysis of the transit time and duration variations caused by the presence of the moon that makes the planet orbit the common center of mass (Kipping 2009a, 2009b). These timing variations would confirm the presence of moons. Finally, by detecting the moon by both methods—photometry and timing variation—it is possible to establish a complete set of physical parameters for the satellite.

The authors acknowledge financial support from the Brazilian agencies CAPES and FAPESP (grant no. 2006/50654-3).

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